

Sta301 current paper 2022 solved by masters

Masters

Virtual University Overseas Examination System V2.1 (x86)

Statistics and Probability (STA301)

Question 33 (Marks: 1)

Attempted 32 Total 52

For a continuous random variable X, $P(X = x)$ is:

Choice

☒ 0

☐ 0.5

☐ 1

☐ 0.4

TIME LEFT

The parameter of the chi- square distribution is.....

Choice

v



$v-1$

$v-2$

$v-p$

If a car is driven on average no more than 1600 Km per month, then formulate the null and alternative hypothesis.

Answer

The Null Hypothesis will be

$$H_0 : \mu \leq 1600 \text{ Km}$$

The Alternative hypothesis will be

$$H_1 : \mu > 1600 \text{ Km}$$

A null hypothesis, generally denoted by the symbol H_0 .

For example, suppose we think that the average height of students in all colleges is 62". This statement

is taken as a hypothesis and is written symbolically as $H_0 : \mu = 62"$. In other words, we hypothesize that $\mu = 62"$

alternative hypothesis denoted by H_1 or H_A

For example, if our null hypothesis is $H_0 : \mu = 62"$, then our alternative hypothesis may be $H_1 : \mu \neq 62"$ or $H_1 : \mu < 62"$.

Null hypothesis

$$H_0 : \mu = 1600 \text{ KM}$$

Alternative hypothesis

$$H_1 : \mu \neq 1600 \text{ Km or}$$

$$H_1 : \mu < 1600 \text{ km .}$$

If you draw all possible samples from some population, calculate the mean for each of the sample and construct the probability distribution of the sample means, what would you have?

Choice

A population distribution

☐

A sample distribution

☐

A sampling distribution

☒

A parameter distribution

☐

For a normal distribution with $\mu=55$ and $\sigma=10$, how much area will be found under the curve to the right of $X=55$?

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Choice

1.0



0.68



0.5



0.32



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All hypothesis tests start with

Choice

☒ A null hypothesis



☐ Alternative hypotheses

☐ Test statistic

☐ Type-I Error

A 95% confidence interval for population proportion p is 32.4% to 47.6%, the value of sample proportion is:

Choice

40%



32.4%



47.6%



80%



In a binomial experiment the total number of trials are:

Choice

☐ Fixed in advance



☐ Changeable according to situation

☒ Unpredictable

☐ Not independent

Suppose there are 5 treatments with 4 blocks in a randomized completed block design. What are the degrees of freedom for blocks?

If the experimental design has k treatments and b blocks, the interaction degrees of freedom are equal to $(k-1)(b-1)$.

for block $b-1$, $4-1=3$

for treatments $k-1$

Choice

2



1



3



4



In case of a 3×3 contingency table what is the value of degrees of freedom?

in the case of a 2 x 3 contingency table, there exist $(2 - 1) (3 - 1) = 2$ degrees of freedom

Choice

2



4



3-1x3-1
2x2
4

6



9



If \bar{X} is the mean of the n observations, then which test statistic will be used to calculate the confidence limits of the population variance σ^2 ?

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Choice

Z-statistic



T-statistic



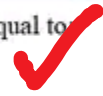
χ^2 -statistics



F-statistics



For $\alpha = 0.01$, the critical values of z for two tailed test are equal to



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Choice

-2.58 and +2.58



-2.33 and +2.33

2%

$\alpha=0.02$



-1.645 and +1.645

$\alpha=0.05$



-1.96 and + 1.96



$\alpha=0.01$



In interval estimation, we always get:

Choice

Single value



Two values



Range of values



Zero



A randomly selected sample of 400 students at university was asked whether or not they will participate in politics. Forty-six percent of the 400 student surveyed answered "yes". Which one of the following statement about number 46% is correct?

Choice

☐ It is a sample statistic.



☒ It is a population parameter.

☐ It is a margin of error.

☐ It is a standard error.

When the random variable X and Y are independent then their co-variance is:

Choice

One

☐

Negative

☐

Zero

☒

Positive

☐

The F-distribution always ranges from:

Choice

0 to 1



0 to $-\infty$



$-\infty$ to $+\infty$



0 to $+\infty$



Which of the following is true for the Poisson distribution:

Choice

☐ mean > variance

☐ mean < variance

☒ mean = variance

☐ mean = standard deviation



In a one-way ANOVA:

Choice

The interaction term has $(c - 1)(n - 1)$ degrees of freedom



An interaction term is given



An interaction effect can be tested



There is no interaction term



Which one of the following assumptions is not a requirement for ANOVA?

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Choice

Dependent samples



Normal populations

random samples

Independent samples

In the case of the sampling distribution of \bar{X} , the finite population correction factor (fpc) is:

Choice

☐
$$\sqrt{\frac{n-N}{N-1}}$$

☐
$$\sqrt{\frac{N-1}{N-n}}$$

☒
$$\sqrt{\frac{N-n}{N-1}}$$

☐
$$\sqrt{\frac{N-n}{N}}$$



The degrees of freedom for a t-test with sample size 6 is:

$$= n - 1$$

Choice

1



3



5



7



Under what condition would you use the paired t-test?

Choice

When there is a single sample of data



When the two samples of data are independent



When the two samples of data are not independent



When there are two proportions



If $f(x, y)$ is bivariate probability density function of continuous random variables X and

Y then marginal density function of y i.e. $h(y)$ is:

Choice

☐ $\int_{-\infty}^{\infty} f(x, y) dx$

☐ $\int_{-\infty}^{\infty} f(x, y) dy$

☐ $\int_{-\infty}^{\infty} \int_{-\infty}^{\infty} f(x, y) dx dy$

☒ $\int_a^b \int_c^d f(x, y) dy dx$



The critical region for $H_1: \mu > \mu_0$ when $\alpha = 0.01$ is:

Choice

☐ $z > z_{0.01}$



☐ $|z| > z_{0.01}$

☒ $z < -z_{0.05}$

☐ $|z| > z_{0.05}$

$$S^2 = \frac{\sum(x - \bar{x})^2}{n}$$

The sample variance is:

Choice

Unbiased estimator of σ^2

☐

Biased estimator of σ^2

☒

Unbiased estimator of μ

☐

Biased estimator of μ

☒

Which one is the formula for calculating the variance of the t-distribution?

Choice

☐ $\sigma^2 = \sqrt{\frac{v}{v-2}}$

☐ $\sigma^2 = \frac{v^2}{v-2}$

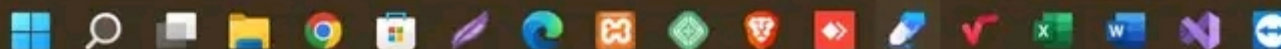
☐ $\sigma^2 = \frac{v}{v-1}$

☒ $\sigma^2 = \frac{v}{v-2}$



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Which one of the formula will be used to find out the confidence interval for μ , when population variance unknown and sample size is large?

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Choice

☐ $\bar{x} \pm Z_{\alpha/2} \frac{s}{\sqrt{n}}$ ✓

☐ $\bar{x} \pm t_{\alpha/2(v)} \frac{s}{\sqrt{n}}$

☒ $\bar{x} \pm t_{\alpha/2(v)} \frac{\sigma}{\sqrt{n}}$

☐ $\bar{x} \pm Z_{\alpha/2} \frac{s}{\sqrt{n-1}}$

The proportion of males in Pakistan is at least 0.48, the alternative hypothesis H_1 is

Choice

$P \leq 0.48$

☐

$P = 0.48$

☐

$P < 0.48$

☒

$P \geq 0.48$

☐

The proportion of working females in Pakistan is at most 0.30, the alternative hypothesis.

Choice

☐ $P < 0.30$



☐ $P = 0.30$

☐ $P \leq 0.30$

☒ $P > 0.30$

To find the confidence interval for the ratio of two variances, we use

Choice

F-Distribution



Z-Distribution



Chi-square-Distribution



t-Distribution



In case of a 2×3 contingency table what is the value of degrees of freedom?

Choice

1

☐

2

☐

5

☒

6

☐

The Chi- Square distribution is continuous distribution ranging from:

Choice

$$-\infty \leq \chi^2 \leq \infty$$



$$-\infty \leq \chi^2 \leq 1$$



$$-\infty \leq \chi^2 \leq 0$$



$$0 \leq \chi^2 \leq \infty$$



What is the shape of t-distribution?

Choice

Bell shaped



J shaped

U shaped

T shaped

For any two estimators T_1 and T_2 , if $\text{VAR}(T_1) < \text{VAR}(T_2)$, then T_1 is:

Choice

☒ Unbiased☐ Sufficient☒ Efficient☐ Consistent

Which of the following is true for the binomial distribution $b(x; n, p)$:

Choice

☐ mean > variance



☐ mean < variance

☒ mean = variance

☐ mean = standard deviation

A 99% confidence interval for the population mean μ is determined to be (65.32 to 73.54). If the confidence level is reduced to 90% the confidence interval for μ

Choice

☒ Become wider☐ Become narrower☐ Remains unchanged☐ None of these

A 95% confidence interval for population proportion p is 32.4% to 47.6%, the value of sample proportion is:

Choice

☒ 40%☐ 32.4%☐ 47.6%☐ 80%

If $\mu_3 = 0.08$ and $\mu_2 = 2.64$, then the skewness of the distribution will be:

$$b_1 = \frac{(\mu_3)^2}{(\mu_2)^3}$$

Choice

2.5

☐

0.87

☒

0.000348

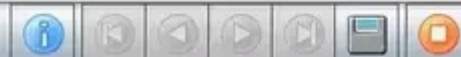
☐

1.5

☐

TIME LEFT

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A hyper geometric random variable is a

Choice

Independent variable

☐

Continuous random variable

☒

Discrete random variable

☐

Variable

☐

$$N(\mu, \sigma^2),$$

In a normal distribution mean deviation is equal to

Choice

$$0.5\sigma$$



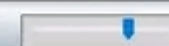
$$0.6745\sigma$$



$$0.7979\sigma$$



$$1.5\sigma$$



If X represents the number of units having the specified characteristic and N is the size of the population, then population proportion p is equal to:

Choice

☐ X/n ☒ N/X ☐ X/N ☒ σ^2 / n

How the standard error is decreased :

Choice

☒ By decreasing the sample size

☐ By decreasing the mean

☐ By increasing the standard deviation

☐ By increasing the sample size



If there are K treatments and R rows in a Randomized Complete Block Design then calculate the total number of experimental units used.

Answer

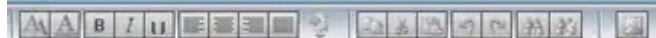
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If there are K treatments and R rows in a Randomized Complete Block Design then calculate the total number of experimental units used

total number of experimental units = $K \times R$

What are the mean and variance of binomial distribution?

Answer



Mean of the Binomial distribution is given by

$E(X)$ which is given by the sum of values which are the result of multiplication of x with $\int x$

whereas variance is given by

Vac =

$$E(X) = np$$

$$VAR(X) = npq$$

From the following joint probability distribution, find $h(1)$.

$x \backslash y$	2	4	$h(y)$
1	0.10	0.15	

Answer

From the following joint probability distribution, find $h(1)$.

$x \backslash y$	2	4	$h(y)$
1	0.10	0.15	1.25
3	0.20	0.30	3.5
5	0.10	0.15	5.25
$g(x)$	0.4	0.6	10

$h(1)$ for the above table is

$$h(1) = 1 + 0.10 + 0.15$$

$h(1) = 1.25$ Ans

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Construct 95% confidence interval for the difference in means $\mu_1 - \mu_2$ in case of paired observations, where

$$\bar{d} = -4.8, s_d = 1.32, t_{0.025(24)} = 2.0639$$

Answer

Construct 95% confidence interval for the difference in means $\mu_1 - \mu_2$ in case of paired observations, where

$$\bar{d} = -4.8, s_d = 1.32, t_{0.025(24)} = 2.0639$$

For the above observations the confidence interval will be

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Let T_1 and T_2 are two unbiased estimators. The variances of both estimators are given below:

$$V(T_1) = \frac{11\sigma^2}{9} \text{ and } V(T_2) = \frac{13\sigma^2}{9}$$

Answer

Let T_1 and T_2 are two unbiased estimators. The variances of both estimators are given below:

$$V(T_1) = \frac{11\sigma^2}{9} \text{ and } V(T_2) = \frac{13\sigma^2}{9}$$

For final estimation, we want to use an *efficient* estimator. Between the two, which estimator is more efficient and why?

The first estimator is more efficient as it will give us less variances than the second one as it is using a multiplication factor of 13

find n and q .

- b) The incident of occupational disease is such that the workers have 30 percent ($P = 30/100$) chance of suffering from 6 workers. Find $P(X=4)$.

Answer



$$P(X = x) = C_x^5 \left(\frac{3}{11} \right)^x \left(\frac{4}{11} \right)^{5-x}$$

- a) From the given binomial probability distribution ,
find n and q .
- b) The incident of occupational disease is such that the workers have 30 percent $P = 30/100$ chance of suffering from 6 workers. Find $P(X=4)$.

$$n=3$$

$$q= 4/11$$

Let x and y are two independent r.v.'s with joint pdf.

$$f(x, y) = \frac{x(1 + 3y^2)}{4},$$

$$= 0, \quad \text{elsewhere.} \quad 0 < x < 2, 0 < y < 1$$

Answer

Let x and y are two independent r.v.'s with joint pdf.

$$f(x, y) = \frac{x(1 + 3y^2)}{4},$$

$$= 0, \quad \text{elsewhere.} \quad 0 < x < 2, 0 < y < 1$$

a. Show that marginal pdf of X is

$$g(x) = \frac{x}{2}; \text{ for } 0 < x < 2$$

b. Also calculate $E(X)$.

page200 example

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Statistics and Probability (STA301)

Question 50 (Marks: 5)

Attempted

52

Total

A random sample of 10 university professors gave their salaries (in thousand Rs.) 13, 11, 19, 15, 22, 20, 14, 17, 14, 15. Another random sample of 5 college professors gave their salaries (in thousand Rs.) 9, 12, 8, 10, 16. Calculate the value of pooled estimator S_p .

Answer

A random sample of 10 university professors gave their salaries (in thousand Rs.) 13, 11, 19, 15, 22, 20, 14, 17, 14, 15. Another random sample of 5 college professors gave their salaries (in thousand Rs.) 9, 12, 8, 10, 16. Calculate the value of pooled estimator S_p .

solution on next page

Masters

$$S_p = \frac{(n_1 - 1)(s_1^2) + (n_2 - 1)(s_2^2)}{n_1 + n_2 - 2}$$

Sample 1 :

$$\begin{aligned}\bar{X} &= \frac{13 + 11 + 19 + 15 + 22 + 20 + 14 + 17 + 14 + 15}{10} \\ &= \frac{160}{10} = 16\end{aligned}$$

$$(X - \bar{X})^2$$

X	$X - \bar{X}$	$(X - \bar{X})^2$	X	$X - \bar{X}$	$(X - \bar{X})^2$
13	3	9	20	4	16
11	5	25	14	2	4
19	3	9	17	1	1
15	1	1	14	2	4
22	6	36	15	1	1

$$\begin{aligned}\sum (X - \bar{X})^2 &= 9 + 25 + 9 + 1 + 36 + 16 + 4 + 1 + 4 + 1 \\ &= 105\end{aligned}$$

$$s_1^2 = \frac{\sum (X - \bar{X})^2}{n_1 - 1}$$

$$= \frac{105}{10 - 1} = \frac{105}{9} = 11.67$$

Sample 2:-

$$\bar{X} = \frac{\sum X}{n}$$

$$= \frac{9+12+8+10+16}{5} = \frac{55}{5} = 11$$

$$\sum (X - \bar{X})^2$$

X	$X - \bar{X}$	$(X - \bar{X})^2$
9	2	4
12	1	1
8	3	9
10	1	1
16	5	25

$$\sum (X - \bar{X})^2 = 40$$

$$S_2^2 = \frac{\sum (X - \bar{X})^2}{n_2 - 1}$$

$$= \frac{40}{5-1} = \frac{40}{4} = 10$$

Put all the value in the form

$$S_p = \frac{(n_1 - 1)S_1^2 + (n_2 - 1)S_2^2}{n_1 + n_2 - 2}$$

$$= \frac{(10-1)(11.67) + (5-1)10}{10+5-2}$$

$$= \frac{(9)(11.67) + (4)10}{13} = \frac{145.03}{13} = 11.16$$